

A Spatially Heterogeneous Expert Based (SHEB) Urban Growth Model Using Model Regionalization

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Abstract

Urbanization changes have been widely examined and numerous urban growth models have been proposed. We introduce an alternative urban growth model specifically designed to incorporate spatial heterogeneity in urban growth models. Instead of applying a single method to the entire study area, we segment the study area into different regions and apply targeted algorithms in each subregion. The working hypothesis is that the integration of appropriately selected region-specific models will outperform a globally applied model as it will incorporate further spatial heterogeneity. We examine urban land use changes in Denver, Colorado. Two land use maps from different time snapshots (1977 and 1997) are used to detect the urban land use changes, and 23 explanatory factors are produced to model urbanization. The proposed Spatially Heterogeneous Expert Based (SHEB) model tested decision trees as the underlying modeling algorithm, applying them in different subregions. In this paper the segmentation tested is the division of the entire area into interior and exterior urban areas. Interior urban areas are those situated within dense urbanized structures, while exterior urban areas are outside of these structures. Obtained results on this model regionalization technique indicate that targeted local models produce improved results in terms of Kappa, accuracy percentage and multi-scale performance. The model superiority is also confirmed by model pairwise comparisons using t-tests. The segmentation criterion of interior/exterior selection may not only capture specific characteristics on spatial and morphological properties, but also socioeconomic factors which may implicitly be present in these spatial representations. The usage of interior and exterior subregions in the present study acts as a proof of concept. Other spatial heterogeneity indicators, for example landscape, socioeconomic and political boundaries could act as the basis for improved local segmentations.

Keywords: Urban Growth Models, Spatial Heterogeneity, Model Fusion, Decision Trees, Denver

1. Introduction

Urbanization is a phenomenon observed since ancient times. It has been strengthened and acquired global magnitude over the last two centuries. More specifically, in year 1800 only 2% of people lived in cities, while in year 1900 the ratio increased to 12%. In year 2008, more than 50% of the world population lived in urban areas [1], and it is estimated that by year 2025 80% of human population will live in cities [2]. This transition has and will change further socioeconomic structure, environmental resource allocation and ecosystem behavior. Urban environmental planning has been quantitatively and qualitatively supported by applying weighted overlay methods

to the driving factors [3], as well as geostatistical techniques as an important part of the GIS-SPRING software capabilities [4]. It is therefore crucial to develop models for urban growth prediction to support interdisciplinary policy decisions for a sustainable future.

Numerous models have been recently developed for land use change prediction (for example [5-9]). The influence of biophysical and socioeconomic factors on land use changes has been an important issue in scientific debates [10] and significant investments are made in the understanding of linkages between ecosystems, climate and land use. For example, the National Science Foundation currently invests \$22.5 million to human-environment research, with a significant portion devoted to land

use models [11].

Typically, land use models examine the likelihood for an area to be transformed from one land type to another [12]. Using available biophysical and socioeconomic variables as driving forces, approaches like linear/logistic regression, and heuristic methods of multicriteria evaluation can be adopted [13-15]. Logistic regression is a special case of generalized linear model, which is used to predict probabilities for the presence or the absence of a specific geographic characteristic. It has been widely used in urbanization [16-18]. In [19] logistic regression was used in order to predict urban-rural land conversion in a multi-temporal environment. Moreover, autologistic regression models have been developed in order to handle spatial autocorrelation. An additional explanatory variable, named autocovariate term can be applied to the logistic regression equation to correct the effect of spatial autocorrelation in a given neighborhood [20-22]. An alternative to the inclusion of spatial autocorrelation in the model expression is the introduction of an optimal sampling scheme to eliminate the spatial autocorrelation within the distance it occurs [19,23].

Other models use fuzzy set theory as a method for dealing with imprecision of the data and determination of class boundaries [24-26]. Algorithms such as support vector machines [27-29] have been successfully applied to land use change modeling. Neighborhood effects are a major factor of land use dynamics [17,30-34] and an important component in many land use change models. The most common method to implement neighborhood interactions in land use change models is cellular automata [35,36], where the transition of a cell from one land use to another depends on the land use of its neighboring cells [37-40].

Artificial Neural Networks (ANNs) model complex relationships between variables, playing an important role as a non parametric approach in land use modeling [41-43] and land use change modeling [44-46]. In [47] a Land Transformation Model was successfully developed where social, political and environmental factors were examined to predict urbanization. This model was further used to forecast land use from 2000 to 2020 and the assessment was achieved using alternative drivers of land use such as forest species [48]. Another approach for future prediction of urban growth has been presented in [49], where the ART-MMAP, a neural network model, produces a prediction map under different scenarios related to historical urban growth data, land use drivers and socioeconomic data. ANNs have been also used for calibration and simulation of cellular automata models in urban systems [50,51]. ANN-based cellular automata models were also proposed for categorizing the cell transition in a binary way (urban/non urban) [52,53]. More-

over, in [54] a generalized approach was introduced for multiple urban uses simulations (e.g. residential, commercial, and industrial).

Decision tree is another non-parametric learning algorithm widely used in land use/land cover modeling [55-59]. Structurally, it differentiates discrete instances, e.g. urban land use categories, through sequentially sorting down a bottom-up tree from the root/upper to the leaf/lower nodes. Each node represents a targeted attribute whose value is determined by a partitioning rule associated to the branch descending from the upper-level node [60]. Compared to generalized linear models, a decision tree is more robust to data distribution such as outliers or missing values, and more flexible in establishing rules that are spatially heterogeneous [61]. Compared to other non-parametric approaches such as ANNs, rules established by decision trees are structurally simple and readily interpretable [55]. However, traditional decision trees treat data as a collection of independent observations, and thus exclude the influence of data spatial autocorrelation in the training process. This limitation has been investigated by a spatial entry-based decision tree designed by [56] where a notion of "spatial entropy" was proposed.

An important aspect of urbanization is spatial heterogeneity [62]. It was soon realized that similar values in an explanatory variable may have different effects in the urban development of different areas and therefore must be treated separately. Although a decision tree universally incorporates a higher degree of spatial heterogeneity, the robustness is yet limited by its intrinsic single-algorithm structure where the complete area is indiscriminately targeted into a global rule [63,64]. Classification and regression trees were used to divide a forested area into homogeneous parts in order to localize the global model [65].

The urban spatial structure and change dynamics can be better described by applying spatial metrics [58,66-68]. Spatial metrics describe spatial heterogeneity by dividing large areas into homogenous subregions. Examples of metrics used to quantify the spatial heterogeneity include patch size, patch density, edge length, distance from nearest neighbor and contagion among others [69]. Moreover, the fractal dimension is also implemented as a spatial metric to describe patch complexity [70,71]. In [72] a region-based system was developed to deal with the spatial and morphologic characteristics of urban structures. Spatial heterogeneity also exhibits scale dependency [73,74]. In [75] a clustering approach was used to map urban influence at multiple scales; the micro, meso and macro scales have been a useful foundation for exploring spatial dynamics of urban structure, addressing spatial, temporal and behavioral complexity

[11].

This paper investigates whether integration of spatially unique models improves on capturing spatial heterogeneity. We investigate whether an expert-based selection of multiple models operating in different spatial regions outperforms a global model with the same input variables (including the segmentation variables) using an identical training dataset. Our implementation includes decision tree classifier and variable training data sizes on a binary urbanization prediction task.

2. Study Area and Modeling Data

2.1. Study Area

The study area is located in the Denver metropolitan area, Colorado, which is in the center of the Front Range Urban Corridor, with the Rocky Mountains from the west and the High Plains from the east. The area selected for this study covers the major part of Denver metropolitan area and is specified by $X_{\min}$: 481862m, $X_{\max}$: 522032m and $Y_{\min}$: 4389809m and $Y_{\max}$: 4421313m (UTM Zone 13 North), as **Figure 1** shows. Denver has experienced a

large urban growth from 1977 to 1997. According to land use maps, provided by the U.S. Geological Survey Rocky Mountain Mapping Centre (<http://rockyweb.cr.usgs.gov/frontrange/datasets.htm>), the percentage of urban growth from 1977 to 1997 was 20.8% (urban areas in 1977: 48% and 1997: 58% of the total study area). This rapid urban growth was the motivation behind this site selection for our model development.

2.2. Response and Predictor Variables

The urban development is the response variable in this current study. The non-developed areas in 1977 that are converted to developed areas in 1997 are assigned as 1 into the response variable, while the non-developed areas 1977 which remain the same in 1997 are given the 0 value. The developed areas in 1977 are excluded from the model and we also assume no conversion from developed back to non-developed area. The urban developed areas include residential areas, commercial/light industries, institutions, communication and utilities, heavy industries, entertainments/recreations, roads and

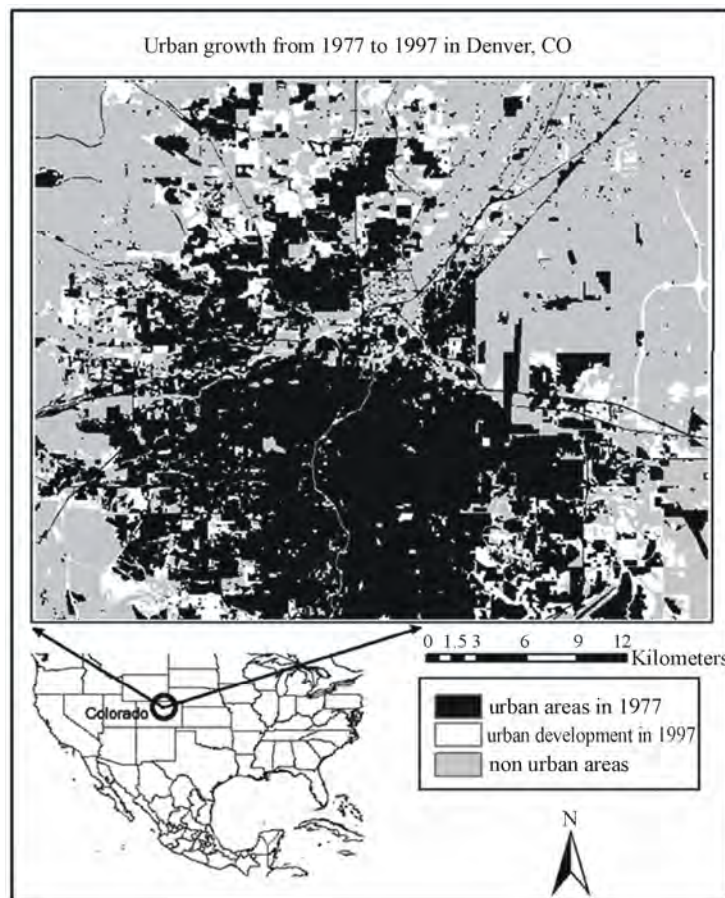


Figure 1. Urbanization changes in the Denver, CO metropolitan area.

other transportation.

We examine 21 predictor variables which are produced using Euclidean distances to the nearest neighbor and Kernel density filters. The predictor variables include: a) Euclidean distance to entertainment venues, heavy industries, rivers, primary roads, secondary roads and minor roads, b) Kernel density (radius: 120 pixel) of agricultural business, residential areas, urban developments, commercial areas, institutes/schools, communications/utilities, lands/ponds, cultivated lands and natural vegetations, c) Kernel density (radius: 10, 30, 50, 80, 100, 150) of distance to urban developments. All the aforementioned variables were based on 1977 vector data, no information from 1997 was incorporated as that was our prediction year. Furthermore, elevation and slope are also considered, making 23 the total number of predictor variables. Statistical analysis in this study area shows that distance to entertainment, density of residential areas, density of urban development and density of natural vegetations contribute with higher importance in modeling the urban growth than the other predictor variables [68]. The final form of the dataset expressing response and predictor variables is in a raster representation with a 30m spatial resolution.

3. Model Development

3.1. Theoretical Underpinnings

Several algorithms have been proposed for urban modeling with varying complexity and success. A motivating factor behind algorithmic selection relies on an algorithm's ability to capture spatial heterogeneity. The current approach is to rely solely on algorithmic complexity to adjust model behavior in different regions of the entire study site. In this paper we examine whether a segmentation of the study area in subregions followed by selective application of methods within each subregion would lead to improved modeling capabilities. In other words through model regionalization we challenge the current expectation that a highly complex globally applied method can sufficiently recognize local heterogeneity and fine tune performance accordingly.

From the model development perspective, we train different models in different subregions and then spatially group the results obtained. These subregions are identified based on expert knowledge on different urbanization drivers. In order to allow a global model to directly compete with our numerous local models the segmentation criterion used to define subregions is also incorporated as an additional input variable to the global model. Therefore the global model has equal opportunity to capture heterogeneity as the local models, because the same input variables and the same modeling techniques

are implemented in both cases.

We apply decisions trees in order to evaluate our hypothesis of multiple local models outperforming a global one. Decision trees are a popular modeling technique as in addition to advanced modeling capabilities, they still remain easy to understand as they can be converted to a set of rules. Decision trees use a training dataset in order to construct the model structure and the produced model is applied to a different dataset (validation) to estimate the prediction accuracy. Of particular interest is performance assessment of local vs. global models on a varying training dataset size. Small training sizes are cost-efficient to acquire but there is an overfitting cost associated with them, therefore the identification of proper balance is investigated.

3.2. Subregion Identification Based on Heterogeneous Behavior

Extraction of homogenous areas is typically based on fragmentation analysis where spatial and landscape metrics are adopted. A wide range of relevant metrics has been proposed, especially in ecological applications [67]. In our case fragmentation analysis involved evaluation of spatial distribution of urban development in the entire study area. It was found that some areas have higher propensity for urban development than others; a consequence of urbanization density. More specifically, an area surrounded by urban structures may experience different development pressures than not surrounded areas [68].

In our study, the entire area is divided into two subregions: the interior urban subregion, a dense urbanized area and the exterior urban subregion with no dense urban structures (**Figure 2**). These two areas exhibit different propensity for urban development.

Figure 3 demonstrates the cumulative probability that an undeveloped pixel in 1977 would be developed in 1997 at a given distance. That relationship is clearly different for the interior and exterior subregions at various distances from already developed areas, which were measured using Euclidean distances between pixel centers. Note that the intention of this graph is to provide a relative comparison between exterior and interior regions leading to motivation behind the model development; the graphs purpose is not to directly incorporate these probabilities in model design. Undeveloped areas in close proximity to existing urban structures are more likely to be converted to urban land use in general, but note that this probability is significantly higher in interior subregions. This is mainly due to the intense human influence which occurs near existed urban structures in dense urban environments such as the interior subregion. For

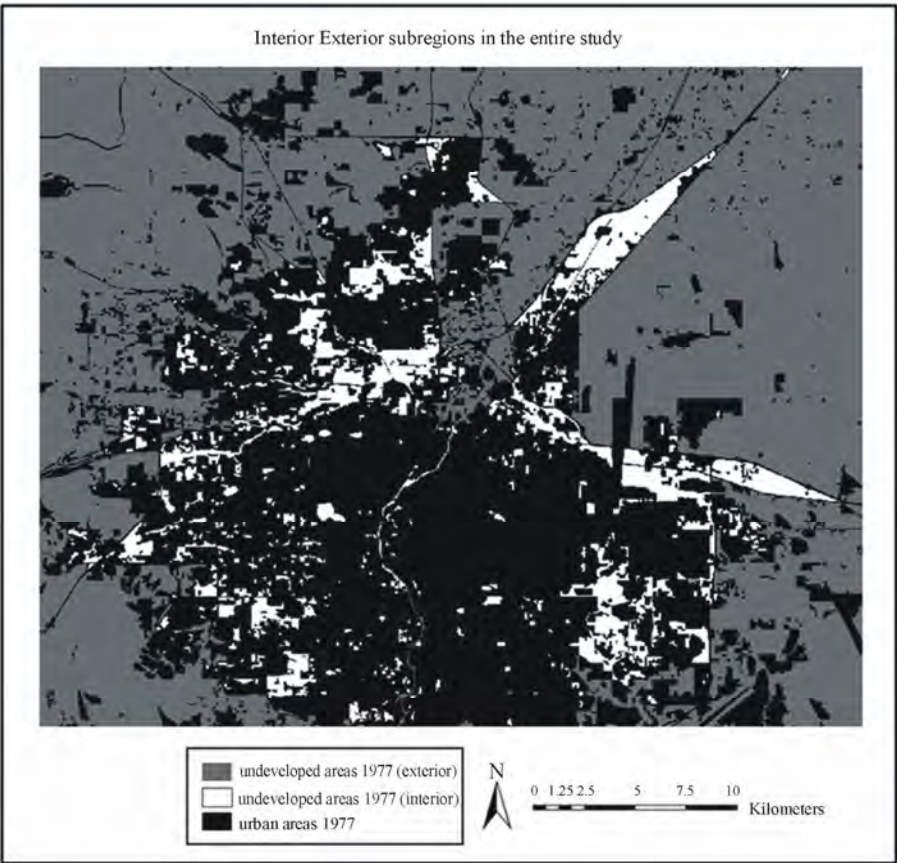


Figure 2. Interior and Exterior subregions of the 1977 Undeveloped area.

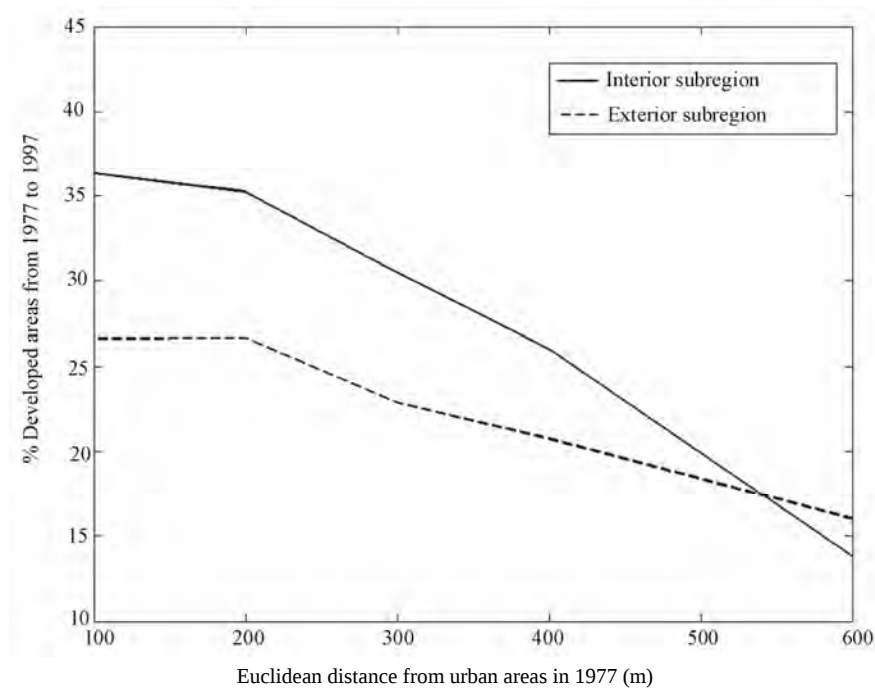


Figure 3. Development probability as a function of Euclidean proximity to existing urban structures for the interior and exterior subregions.

example, the commercial value of these properties may be higher than places far away from buildings. Therefore, the decision to separate in the proposed models interior and exterior areas reflects expert knowledge on expected urban development behavior.

Motivated by the divergence in urban development behavior we develop the proposed local models for each subregion (one for the interior and another for the exterior) and contrast them with a global model trained and operating in both subregions simultaneously. Further segmentations are possible, especially for the exterior subregion, however this interesting investigation is reserved for future work. The purpose of this manuscript is to demonstrate the proof of concept on model regionalization and excite additional research.

3.3. Model Design and Experimental Setup

The proposed Spatially Heterogeneous Expert Based (*SHEB*) model uses multiple decision trees to capture urban growth. The entire study area is divided into the interior and exterior subregions leading to the creation of multiple models to test model regionalization benefits. If a model is trained using samples exclusively from a subregion it is called *Local*, if samples come from the entire study area the name *Global* is assigned. We also use a subscript index in the naming structure to reflect where the model is simulated for validation purposes, for example *Global_{int}* relates to a globally trained model validated only in the interior subregion. All the *Local* models are trained and validated exclusively in the same subregion, therefore the notation *Local_{int}* for example suggests a local model trained and validated in the interior subregion. As a result of the above we have developed the following models:

- *Local_{int}*: training and validation dataset from the interior subregion.
- *Local_{ext}*: training and validation dataset from the exterior subregion.
- *Global_{int}*: training dataset from the entire study area, validation dataset only from the interior subregion.
- *Global_{ext}*: training dataset from the entire study area, validation dataset only from the exterior subregion.
- *Global_{all}*: training and validation dataset from the entire study area.

We should clarify that *Global_{int}*, *Global_{ext}* and *Global_{all}* are the exact same model since they are all produced from the same training set from the entire study area; however, model performance is validated in different regions to allow comparisons with the corresponding *Local* models.

In order to identify the optimal balance between *Local* and *Global* models we perform comparisons in each

subregion (interior and exterior) and in the overall site (all region). The term balance is used to refer to the fact that not always *Local* models will outperform global ones; in every region we compare the corresponding *Local* with the *Global* model and decide which one to use. The subregion analysis lead to the following pairwise comparisons: a) *Local_{int}* and *Global_{int}*, b) *Local_{ext}* and *Global_{ext}*. For each subregion, the comparison between the *Local* and *Global* models assesses whether spatial heterogeneity should be addressed separately in that region. Depending on the subregion accuracy assessment the predominant subregion-specific model is selected to participate further into the *SHEB* model structure. Since the *SHEB* model expects to operate over the entire study site it is compared against the *Global_{all}* model. These comparisons are presented graphically in **Figure 4**.

3.4. Algorithmic Specifics

The decision tree models were developed and evaluated in the Matlab environment. Ten observations were set as the minimum for a node to be split. Moreover, each decision tree is adjusted using a 10-fold cross-validation and a pruning process.

In order to compare *Local* and *Global* models we had to ensure comparable model complexity and input selection. Regarding input selection the *Local* models contain the aforementioned 23 predictor variables (see section 2.2). The *Global* models incorporate the exact same 23 variables plus an additional predictor variable: a dummy variable with value of 1 if a point belongs to the interior subregion and the value of -1 if it lies in the exterior subregion. By doing so, the *Global* models have the potential to express the expert-derived interior/exterior segmentation within their model structure. In terms of model complexity the decision trees developed for *Local* and *Global* models are directly comparable because the training of each model took place considering the same minimum number of points (10 points) classified in every leaf.

The reference output variable is dichotomous, with value 1 if the change is from non-urban in 1977 to urban in 1997, and 0 when the 1977 non-urban areas do not change. The reference output binary variable is compared with the predicted output of *SHEB* and *Global_{all}* models. Each set of predictor values is inserted into the decision tree, which is produced using the regression tree option in Matlab, and a corresponding response value is predicted. Because the reference response variable contains only two numeric values, 0 and 1, the corresponding predicted output is a continuous variable with a range between 0 and 1, indicating the probability for change. The closer the probability to 1, the more likely

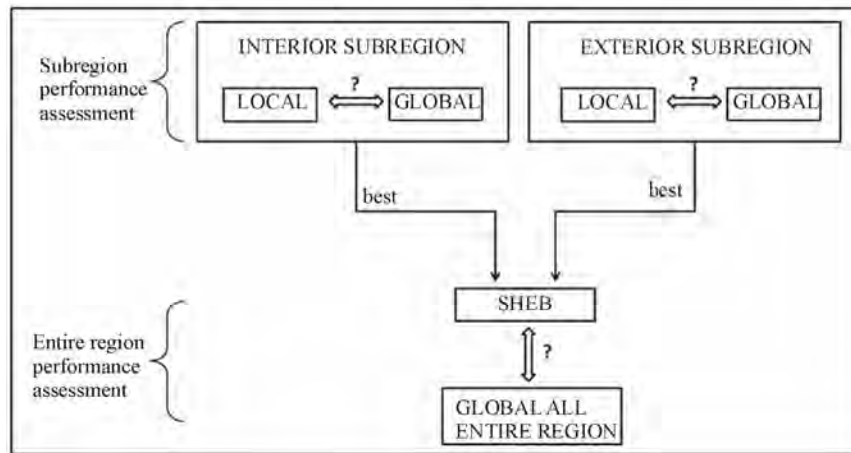


Figure 4. Design scheme of SHEB urban growth model.

this area is to experience urban development. A threshold is applied in order to categorize the values of the predicted output into two classes: 0 and 1. In most cases, a 0.5 threshold is used, so as values greater than 0.5 to be classified to 1 (developed), otherwise to 0 (non-developed). This value of 0.5 was used as threshold in our study as well.

3.5. Training Sample Specifics

From the entire study area (710,536 points) we extracted 70% of the data points for validation purposes (497,375 points) and kept the remaining 30% for various training experiments. The validation dataset contained 389,810 no change and 107,565 change points; spatially it was distributed to 59,755 interior points and 437,620 exterior points. All statistics reported in the results section are calculated using the same validation dataset.

We examined a variety of training sample sizes to assess model performance. We varied the training sample from 4000 to 30000 with an increment of 4000 leading to 14 different training sets. For a given training sample total size goal (e.g. 4000 total training points), we randomly selected equal number of interior and exterior training points (e.g. 2000 for each). Each *Local* model was trained with the corresponding points (e.g. the 2000 interior points for the *Local_{int}* model) and the corresponding *Global* model used the identical points from the two *Local* models combined (e.g. the 2000 interior points for the *Local_{int}* model and the 2000 exterior points for the *Local_{ext}* model leading to the 4000 point training dataset for the *Global* model). Identical points were used to support direct comparison between *Local* and *Global* models. Furthermore, for each training dataset total size (e.g. 4000) we performed 50 random sampling selections to limit bias especially in smaller size datasets.

Semivariograms analysis showed that spatial autocor-

relation exists within 450m. In order to overcome this difficulty, training sets were produced using several random samplings, all at least 450m apart from each other. Because of the reduced number of training points, high overfitting occurred with large discrepancies between calibration and validation accuracies. Therefore, the spatial autocorrelation is not considered in this paper and any point could participate in model calibration/validation.

4. Results

Results from each subregion are presented in the subregion performance assessment section. Using these results as a guide, a proposed *SHEB* model is created and contrasted with a *Global* model leading to the entire region performance assessment. The aggregation statistics in the entire region put equal weight to both interior and exterior subregions to avoid a site-dependence bias. We should note that the term prediction relates to the extrapolation on historical data at later times.

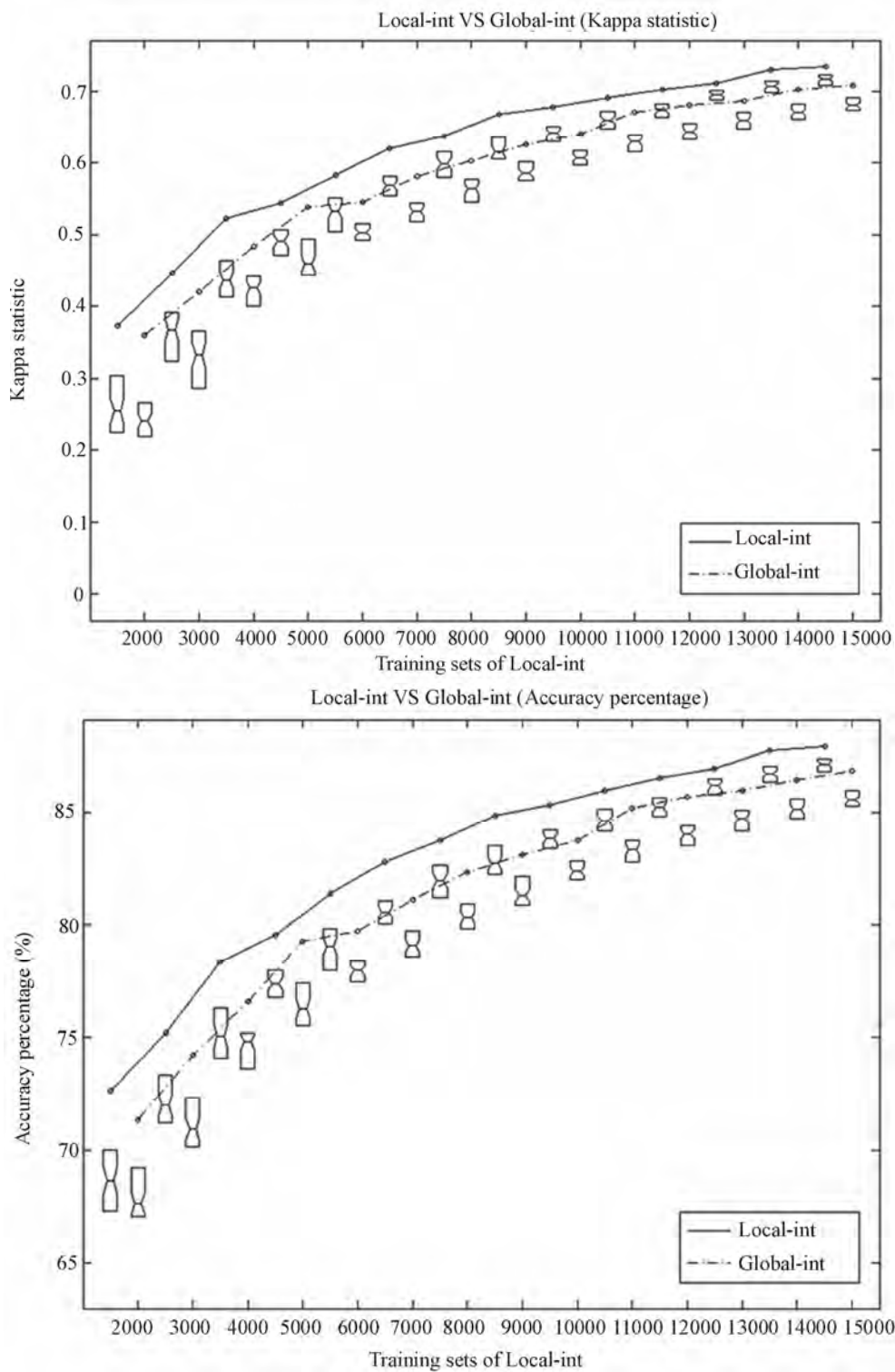
4.1. Interior and Exterior Subregion Performance Assessment

The performance of *SHEB* model is evaluated using the confusion matrix and the Kappa statistic. Confusion matrix is produced by cross-tabulation between predicted and actual variables [76,77]. It is the percentage of predicted cases which are correctly classified either as urban or non urban areas. Kappa statistic is a more robust method in classification accuracy, because it can provide concordance avoiding the cases which are correctly classified by chance [78].

In Figure 5 the accuracy results (Kappa, accuracy percentage) in the interior and exterior subregions are graphically displayed by boxplots. Each box contains the

median value (central mark) and the 25th and 75th percentiles (edges of the box) for 50 random training sets. The graph presents pairs of local and global models and they are slightly offset for visualization purposes. Every

pair of local-global is associated with a certain training sample size that is presented on the X axes. The training sets of SHEB models for each subregion (interior/exterior) vary from 2000 to 15000 points providing a



(a)

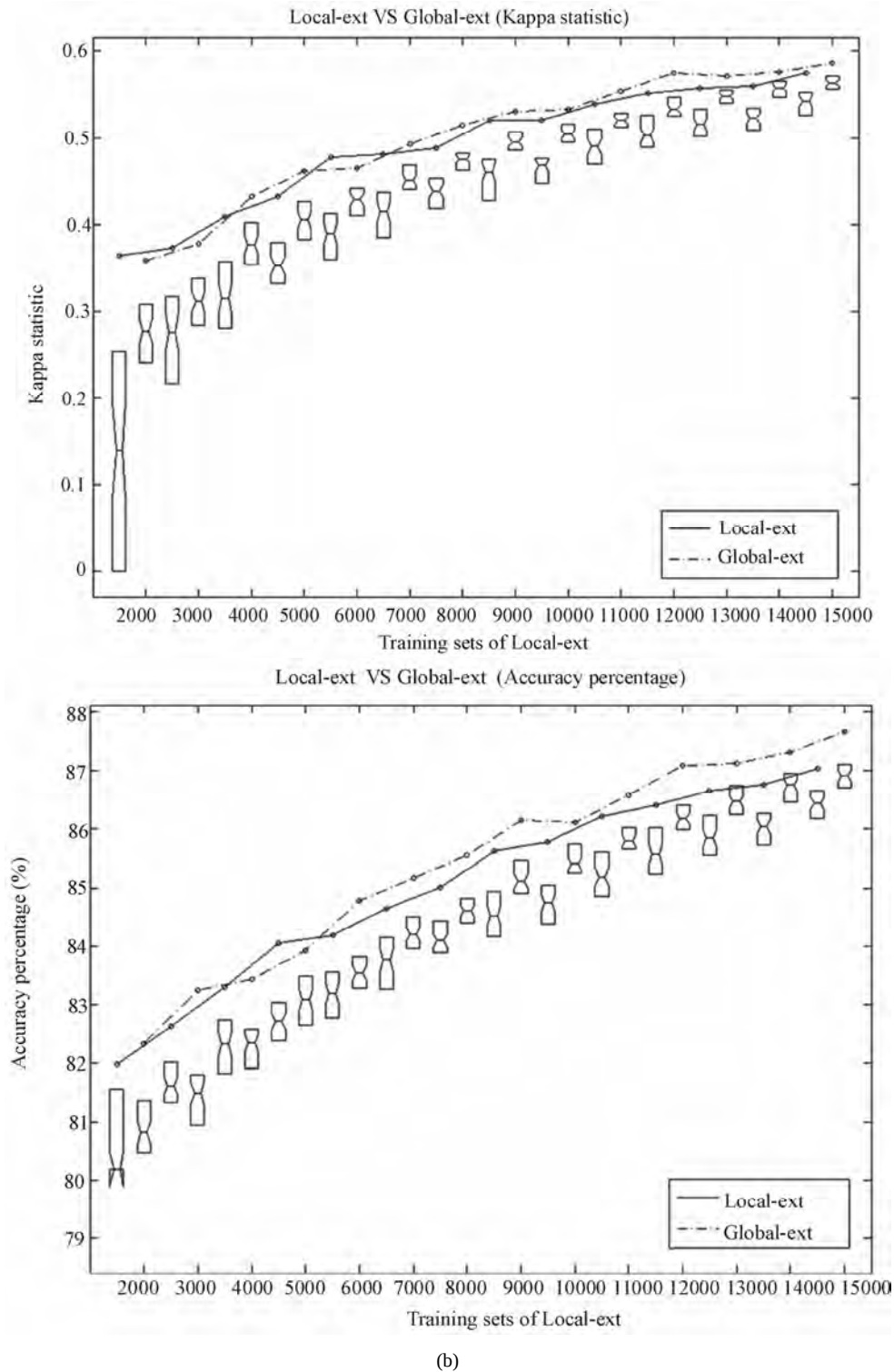


Figure 5. Comparison between *Local* and *Global* models using decision tree algorithms. (a) Decision trees assessment within the interior subregion; (b) Decision trees assessment within the exterior subregion.

total from 4000 to 30000 points; the exact same points are used in the corresponding *Global* models. Fifty different decision trees are produced for each training size.

This process minimizes the bias regarding the randomness of training set selection. Moreover, a line connecting the maximum value of Kappa and accuracy percent-

age for each training size is drawn.

The comparison within the interior subregion using models $Local_{int}$ and $Global_{int}$ for both Kappa and accuracy percentage in different training sizes is given in **Figure 5(a)**. The comparison in the exterior subregion between $Local_{ext}$ and $Global_{ext}$ is presented in **Figure 5(b)**. In the interior subregion, the $Local_{int}$ model exhibits significant improvements over the $Global_{int}$, while the results for the exterior subregion do not show significant differences between the $Local_{ext}$ and $Global_{ext}$ models.

4.2. Entire Region Performance Assessment

4.2.1. Single Pixel Assessment

Using the subregion performance assessment we fuse the *Local Interior* model ($Local_{int}$) with the *Global Exterior* model ($Global_{ext}$) to formulate the proposed *SHEB* model. The *SHEB* is then compared to a decision tree-based *Global* model ($Global_{all}$) operating on the entire study area. Since both *SHEB* and *Global* model use the same model to classify points in the exterior subregion, algorithmic improvements are due to any performance differences in the interior subregion. We average improvements over both regions to produce the overall accuracy and Kappa statistics comparisons of **Figure 6**. It is worth mentioning that in decision tree graphs (**Figures 5 and 6**), both Kappa and accuracy percentage are sensitive to the number of training points, as expected. In order to examine the significance of Kappa statistic as well as the accuracy percentage in the two pairwise comparisons (*SHEB* VS $Global_{all}$), a paired Student's t-test is carried out. The comparison aggregates differences between the best two models for each training dataset size. This test is used to investigate performance relationship between two models, without considering any one-to-one correspondence between points belonging into the same group. According to **Table 1**, *SHEB* model differences from the *Global* model in terms of both Kappa and accuracy percentages are statistically significant ($\alpha=0.05$). In addition, the negative t values for the exterior subregion justify the selection of the *Global* over the *Local* model to participate in the *SHEB* model.

4.2.2. Neighborhood Assessment

The above accuracy metrics are based on a pixel per pixel comparison between model output and reference data. Multi-scale accuracies are also used to aggregate performance within a neighborhood moving away from individual pixels. The multi-scale accuracies capture the similarity of patterns providing an assessment in different resolutions. More specifically, the multi-scale accuracy assesses the number of changes occurred in a specified window versus the actual number of changes with-

out taking into account the exact spatial specificity of these changes as long as they take place within a local neighborhood. This assessment technique is important and beneficial for potential users such as policy makers and planners, where algorithmic performance in a given window (e.g. a 1 mile block) is more desirable rather than the actual locations of urban sprawl within that neighborhood. The calculation is defined by the following formula [79].

$$F_{i,d} = \frac{\sum_{i=1}^n \left| 1 - \frac{m_{i,d} - \bar{m}_{i,d}}{M_{i,d}} \right|}{n}$$

where $F_{i,d}$ is the accuracy of the pixel i in a window with d diameter size of the circular window within which the accuracy is calculated, $m_{i,d}$ is the actual changes occurred in d , $\bar{m}_{i,d}$ is the predicted changes in d , $M_{i,d}$ is the total valid pixels (excluding the existing urban developed pixels in 1977) in the examined window and n is the total population of pixels.

In **Figure 7**, the graphs of multi-scale accuracies are presented using the training sets of 4000, 16000 and 30000 points for both *SHEB* and $Global_{all}$ models. For each training size test, the best algorithm of the 50 decision trees was selected in order to calculate the multi-scale accuracies. The size of neighborhood ranges from 3x3 to 70x70 pixels (90m to 2100m). The fusion between $Local_{int}$ and $Global_{ext}$ (*SHEB* model) offers increased accuracy when compared to the $Global_{all}$ model. For example, at the 1km scale, a representative planning scale for the urban community, accuracy improvement varies from 1% to 3%. Most importantly, improvements are more significant for smaller training set sizes, which makes the proposed method even more appealing considering that data availability is a typical limitation in such models.

5. Discussion and Conclusions

A Spatially Heterogeneous Expert Based (*SHEB*) model, which addresses spatial heterogeneity using multiple region-specific models, is introduced in this research. Our hypothesis investigates whether expert knowledge improves prediction accuracy through model regionalization, in other words whether the integration of different models in homogeneous local subregions outperforms a global model trained in the entire study area. Most similar studies capture the spatial heterogeneity using the differentiated factor, the factor which describes this dissimilarity, as an additional term to a global model applied in the entire study area. In contrast, the *SHEB* model uses this expert knowledge prior to the model ap-

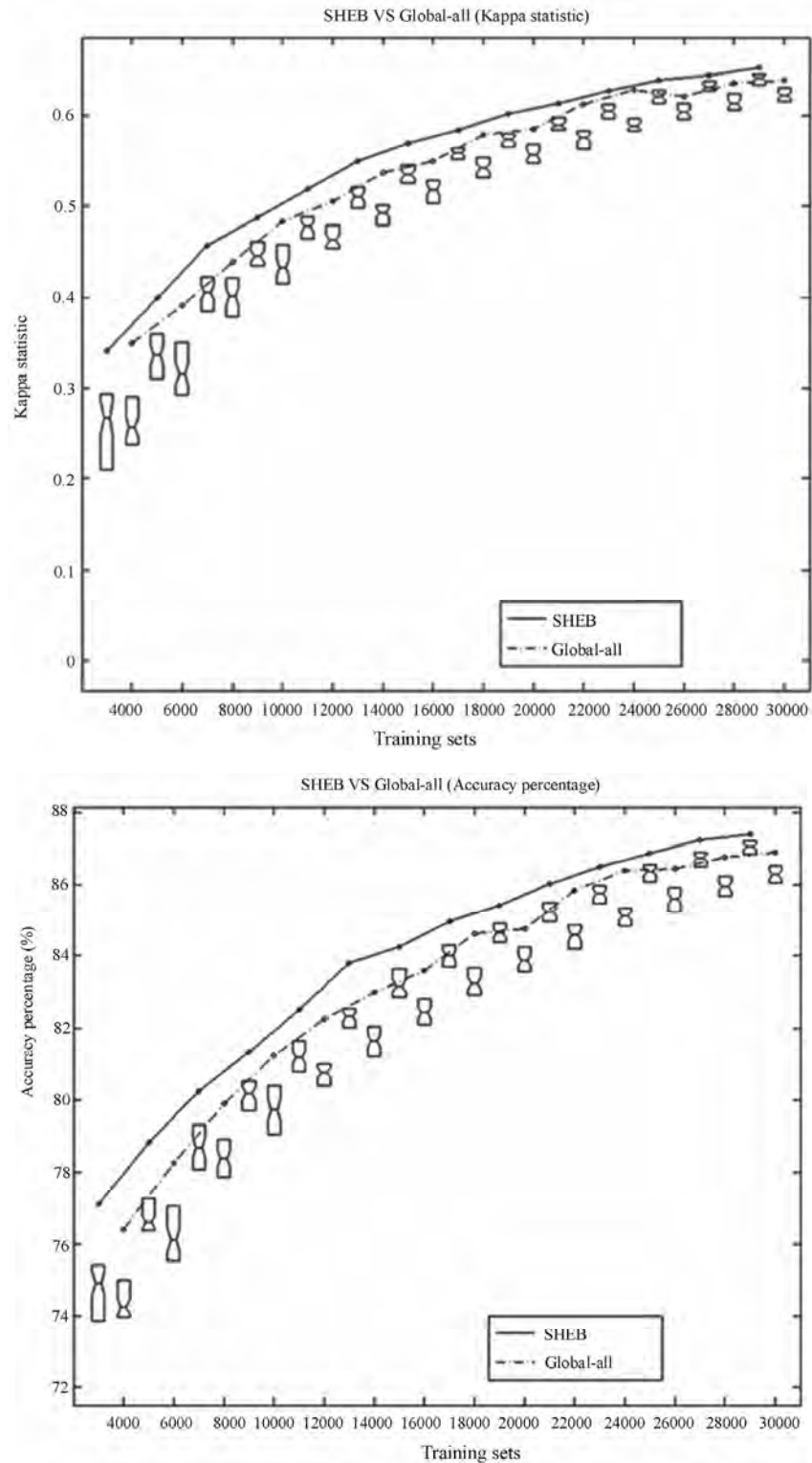


Figure 6. Prediction accuracy of the *SHEB* model versus *Global* model.

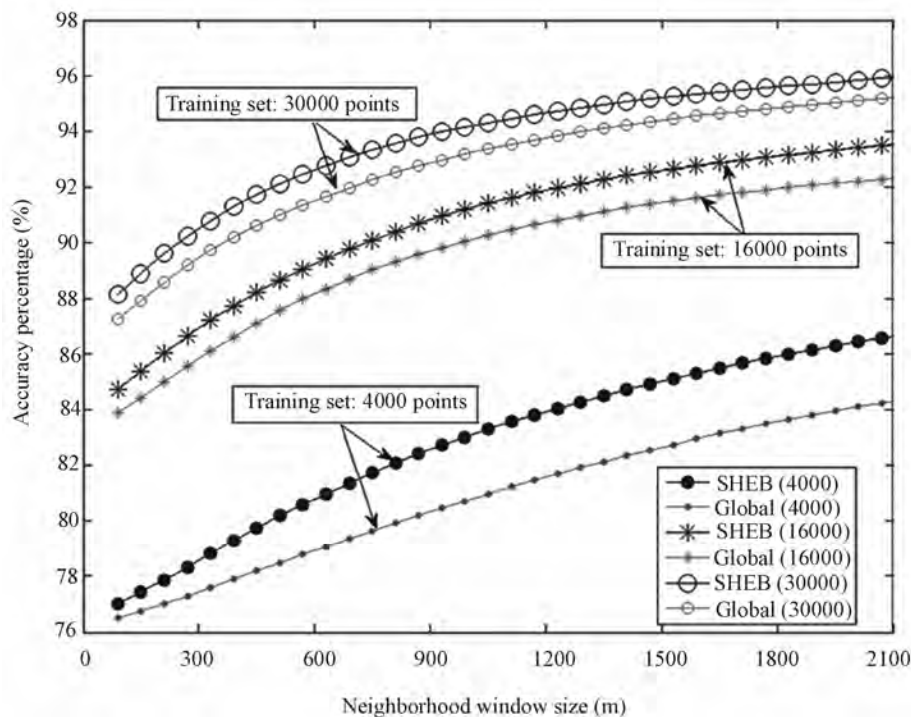
plication, divides the study area into homogenous subregions, and then applies different models in each subregion. This alternative approach in urban growth model-

ing produces higher accuracy results than a globally trained and applied model.

More specifically, using decision trees as the underly-

Table 1. Student's t-test for decision trees.

Model Comparisons	Performance metric	t-value	p
<i>SHEB</i> vs. <i>Global_{all}</i>	<i>Kappa</i>	4.294	8.73E-04
	<i>accuracy percentage</i>	7.258	6.38E-06
<i>Local_{int}</i> vs. <i>Global_{int}</i>	<i>Kappa</i>	9.944	1.92E-07
	<i>accuracy percentage</i>	10.541	9.73E-08
<i>Local_{ext}</i> vs. <i>Global_{ext}</i>	<i>Kappa</i>	-4.148	1.10E-03
	<i>accuracy percentage</i>	-7.642	3.68E-06

**Figure 7. Multi-scale accuracy comparison between proposed (SHEB) and benchmark (Global) models using 4000, 16000 and 30,000 training points.**

ing algorithmic classifier, the developed local models, suitably aggregated, produce improved prediction results than a single global model. The fusion of *Local Interior* model (*Local_{int}*) and the *Global Exterior* model (*Global_{ext}*) was more accurate than a decision tree-based *Global* model.

Different sizes of training sets exhibited different accuracies in both Kappa and accuracy percentages. As expected, the larger the training set, the better the model accuracy performance. It is interesting to point out that the rate of accuracy improvement with increases in training size was higher for the interior model, suggesting a larger heterogeneity within that subregion. There was also a saturation point where further training sizes increases resulted in minor accuracy improvements. More specifically, the improvement in Kappa for different training sample sizes was approximately 1.0 and 1.5 (out of 100) for maximum and average values respectively. The corresponding differences of accuracy per-

centages are 0.4 % and 0.6% at the pixel level. A t-test comparison also supported our model selection suggesting the statistical significance of these improvements. Most importantly for urban planning purposes, this improvement reaches approximately 3% at the 1km modeling scale and for small training datasets. Therefore, using the proposed methodology, we can obtain satisfactory accuracies when working in large neighbourhoods, especially when the training sample size is small. The latter is desirable for urban planners because restricted data availability is a common problem in such projects. We should note that even though the decision tree method offered significant statistical improvements, it did not exhibit any over/under performance in specific localized areas suggesting that further model segmentation may be difficult.

Incorporation of spatial heterogeneity is important for planning urban development and designing the appropriate location for establishing new facilities. The unique-

ness of a subregion can be identified not only by characteristics on its spatial and morphological properties, but also based on socioeconomic factors which may be implicitly present in these spatial representations. An interesting future investigation could base model regionalization on socioeconomic and administrative variables. For example, different models could be based on governing units that inherently may behave differently. The local information can provide reliable modeling adaptability because expert knowledge can more easily be incorporated in homogenous subregions rather than in the entire study area. The *SHEB* model can sufficiently support the applicability of different homogenous subregion extractions, in order to handle the spatial heterogeneity. The usage of interior and exterior subregions in the present study acts as a proof of concept. Introducing further spatial heterogeneity into the model could potentially lead to further improvements in the prediction accuracy of urban development.

6. Acknowledgements

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